

Binomial Distribution

Worksheet

binompdf(n,p,x)

(1) Compute the probability of X successes, using the binomial formula.

(a) $n = 5, X = 2, p = 0.025$

```
binompdf(5,.025,
2)
.0057928711
```

(b) $n = 12, X = 6, p = 0.45$

```
binompdf(12,.45,
6)
.2123846821
```

(c) $n = 6, X = 0, q = 0.35$

```
1-.35
binompdf(6,.65,0)
.0018382656
```

(d) $n = 45, X = 10, p = 0.25$

```
binompdf(45,.25,
10)
.1289319305
```

(e) $n = 22, X = 20, p = 0.68$

```
binompdf(22,.68,
20)
.01057037
```

(2) Compute the probability of X success given $n = 12$ and $p = .45$ using the binomial formula.

(a) $P(X = 6)$

```
binompdf(12,.45,
6)
.2123846821
```

(b) $P(X \geq 9)$

$P(9) + P(10) + P(11) + P(12)$

```
binompdf(12,.45,
9)+binompdf(12,.
45,10)+binompdf(
12,.45,11)+binom
pdf(12,.45,12)
.0355748675
```

(c) $P(X < 4)$

$P(0) + P(1) + P(2) + P(3)$

```
binompdf(12,.45,
0)+binompdf(12,
.45,1)+binompdf(1
2,.45,2)+binompd
f(12,.45,3)
.1344680692
```

(d) $P(4 < X < 7)$

$P(5) + P(6)$

```
binompdf(12,.45,
5)+binompdf(12,.
45,6)
.4348829206
```

(e) $P(5 < X < 7)$

$P(6)$

```
binompdf(12,.45,
6)
.2123846821
```

(3) A student randomly guesses at 10 multiple choice questions. Each question has four possible answers with only one being correct, and each is independent of every other question.

$n=10$ $p = \frac{1}{4} = .25$

(a) Find the probability that the student guesses EXACTLY 4 correct.

$\text{binompdf}(10,.25,4) = 0.145998$

(b) Find the probability of guessing less than 3 correctly.

$P(0) + P(1) + P(2) = 0.5255928$

(c) Find the probability of guessing 8 or more.

$P(8) + P(9) + P(10) = 4.1 \times 10^{-4} = .00041$

(d) Find the probability of guessing between 4 and 6 inclusively.

$P(4) + P(5) + P(6) = 0.2206192$

```
(a) binompdf(10,.25,
4)
.1459980011
```

```
(b) binompdf(10,.25,
0)+binompdf(10,.
25,1)+binompdf(1
0,.25,2)
.525592804
```

```
(c) binompdf(10,.25,
8)+binompdf(10,.
25,9)+binompdf(1
0,.25,10)
4.15802002E-4
```

```
(d) binompdf(10,.25,
4)+binompdf(10,.
25,5)+binompdf(1
0,.25,6)
.2206192017
```

(4) In a Gallop Poll conducted January 30 – February 2, 2008, 43% of 18-29 year olds said that they were worried about retirement. Find the probability that out of 15 college students aged 18 – 29.

(a) Exactly 1 is worried about retirement.
 $P(1) = \text{binompdf}(15, .43, 1) = 0.0024648$

```
(a) binompdf(15,.43,
1)
.0024649476
```

(b) Fewer than 5 are worried about retirement.
 $P(0) + P(1) + P(2) + P(3) + P(4) = 0.1545517$

(c) At least 10 are worried about retirement.
 $P(10) + P(11) + P(12) + P(13) + P(14) + P(15) = 0.056459$

(d) Between 8 and 10 inclusively are worried about retirement.
 $P(8) + P(9) + P(10) = 0.272356$

```
(b) binompdf(15,.43,
0)+binompdf(15,.
43,1)+binompdf(1
5,.43,2)+binompd
f(15,.43,3)+bino
mpdf(15,.43,4)
.1545517468
```

```
(c) binompdf(15,.43,
10)+binompdf(15,
.43,11)+binompdf
(15,.43,12)+bino
mpdf(15,.43,13)+
binompdf(15,.43,
14)+binompdf(15,
.43,15)
.0564591584
```

```
(d) binompdf(15,.43,
8)+binompdf(15,.
43,9)+binompdf(1
5,.43,10)
.2723560899
```

(5) In Gallop Poll, 35% of 30-49 year olds stated they believed in ghosts. Find the probability that out of 16 college students aged 30-49

(a) Exactly 5 said they believed in ghost.
 $P(5) = \text{binompdf}(16, .35, 5) = 0.200756$

(b) Exactly 5 said they do not believe in ghosts.
 $1 - 0.35 = 0.65$
 $P(5) = \text{binompdf}(16, .65, 5) = 0.0048932$

(c) At least 4 believe in ghosts.
 $P(0) + P(1) + P(2) + P(3) = 0.13385965$
 $P(X \geq 4) = 1 - 0.13385965 = 0.86614035$

(d) At least 4 do not believe in ghosts.
 $P(0) + P(1) + P(2) + P(3) = 2.3854 \times 10^{-4} = 0.00023854$
 $P(X \geq 4) = 1 - 0.00023854 = 0.9997614587$

```
(a) binompdf(16,.35,
5)
.2007565735
```

```
(b) binompdf(16,.65,
5)
.0048932556
```

```
(c) binompdf(16,.35,
0)+binompdf(16,.
35,1)+binompdf(1
6,.35,2)+binompd
f(16,.35,3)
.13385965
```

```
(d) binompdf(15,.65,
0)+binompdf(15,.
65,1)+binompdf(1
5,.65,2)+binompd
f(16,.65,3)
2.385412877E-4
```